

Study of Novel Microstrip Graphene Nano Patch Antenna - 'GNPA' for Terahertz Radiation



¹Gaurav Tewari, ²Rajveer Singh Yaduvanshi

Abstract

Graphene is best material as compared to several conventional metallic material. The scattering of terahertz radiation on a graphene-based microstrip nano-patch antenna is numerically analyzed. The extinction cross section of the nano-antenna supported by silicon and silicon dioxide substrates of different thickness are calculated. Scattering resonances in the terahertz band are identified as Fabry–Perot resonances of surface plasmon polaritons supported by the graphene film. A strong tunability of the antenna resonances via electrostatic bias is numerically demonstrated, opening perspectives to design tunable graphene-based nano-antennas. These antennas are envisaged to enable wireless communications at the nanoscale.

Keywords: GNPA; Scattering; Terahertz radiation

1. Introduction

Graphene has recently attracted intense attention of the research community due to its extraordinary mechanical, electronic and optical properties [1]. Being a flat monolayer of carbon atoms tightly packed in a two-dimensional honeycomb lattice, graphene allows to utilize novel physics in a plethora of potential applications, ranging from ultra-high-speed transistors [2] to transparent solar cells [3], meta-materials [4] and graphene plasmonics [5–9].

One particularly promising research field is that of graphene-enabled wireless communications.

Wireless For these reasons,

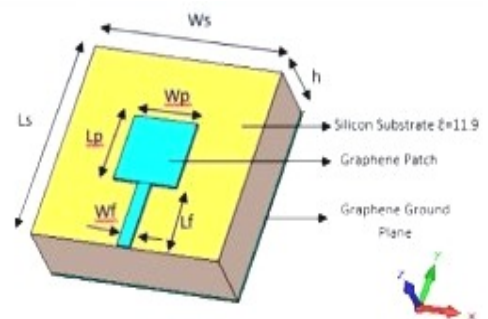


Fig. 1. Sketch of the graphene-based nano-antenna under consideration

using micrometer- size metallic antennas to implement wireless communications among nanosystems becomes unfeasible. However, owing to its ability to support surface plasmon polaritons (SPP) [10,11],



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graphene is seen as the enabling technology for this emerging field. Indeed, a graphene-based nano-patch antenna with lateral dimensions of just a few micrometers is predicted to resonate in the terahertz band [12,13], at a dramatically lower frequency and with a higher radiation efficiency with respect to their metallic counterparts. In consequence, graphene-based nano-antennas are envisaged to enable wireless communications among nanosystems [14] In this work, we present a systematic numerical analysis of the terahertz radiation scattering on a graphene-based nano-patch antenna (Fig. 1). A graphene rectangular patch with length L and width W supported by a dielectric substrate of thickness D is illuminated by a plane wave linearly polarized along the patch length. The associated scattering problem is then solved numerically, and the extinction, absorption and scattering cross sections are analyzed. The remainder of this paper is organized as follows. In Section 2, the expression used to model the electric conductivity of graphene is presented. In Section 3, two different approaches to model a graphene patch are described and compared. Next, in Section 4, the cross sections of the graphene-based nano-antenna are obtained, and Section 5 explores their dependence on several parameters, such as the antenna dimensions or the chemical potential. Finally, Section 6 concludes the paper.

2. Conductivity Evaluation of Graphene

Material:

Graphene-based nano-patch antennas are envisaged to have a length and width in the order of a few micrometers [12,13]. Since it has been experimentally demonstrated that edge effects on the graphene conductivity only appear

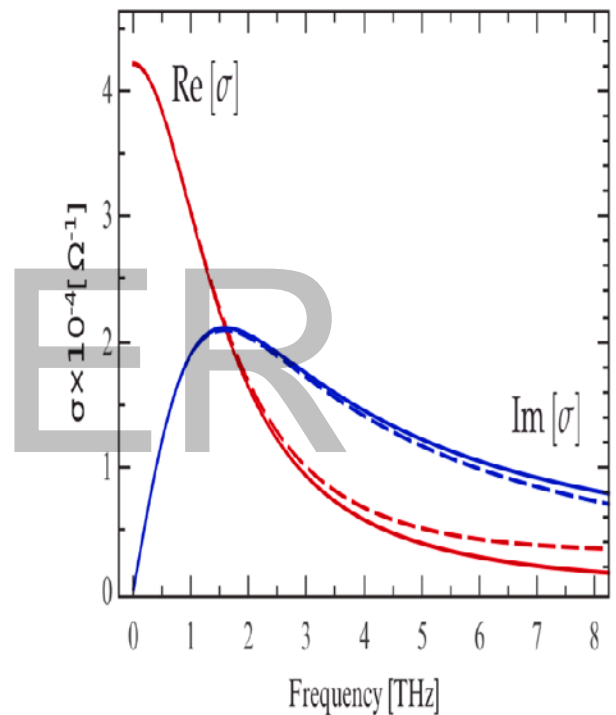


Fig. 2. Real and imaginary part of the total conductivity (solid lines) and the intraband conductivity (dashed lines) at room temperature ($T = 300$ K) and zero electrostatic bias ($m_c = 0$ eV).

in structures with lateral dimensions considerably smaller than 100 nm [15], in this analysis we will disregard the edge effects and will use the electrical

conductivity model developed for infinite graphene sheets [10,11]. The surface conductivity of an infinite graphene film can be calculated by means of the Kubo formalism [10,11].

Within the random-phase approximation, the surface conductivity can be represented in a local form with the Drude-like intraband contribution

$$\sigma(\omega) = \frac{2e^2 k_B T}{\pi \hbar} \ln \left[2 \cosh \left[\frac{\mu_c}{2k_B T} \right] \right] \frac{i}{\omega + i\tau^{-1}}, \quad \dots(1)$$

and interband contribution given by

$$\sigma_i(\omega) = \frac{e^2}{4\hbar} \left(H\left(\frac{\omega}{2}\right) + i \frac{4\omega}{\pi} \int_0^\infty d\epsilon \frac{H(\epsilon) - H(\omega/2)}{\omega^2 - 4\epsilon^2} \right).$$

Here $\tau = 1013$ s is the relaxation time, T is the temperature, μ_c is the chemical potential and $H(x) = \frac{1}{2} + \frac{1}{\pi} \arctan(x)$ is defined as:

$$H(\epsilon) = \frac{\sinh(\hbar\epsilon/k_B T)}{\cosh(\mu_c/k_B T) + \cosh(\hbar\epsilon/k_B T)}.$$

In the frequency region of interest (below 5 THz), the intraband contribution (1) dominates [16]. This can be seen in Fig. 2, where the frequency dependence of the real and imaginary part of the intraband conductivity s and the total conductivity $s_{total} = s + si$ are compared at room temperature ($T = 300$ K) and zero electrostatic bias ($\mu_c = 0$ eV). In the following, we neglect the interband conductivity contribution and assume the conductivity of the graphene patch to be purely intraband.

3. Formulations Used

In order to find the electromagnetic field scattered by a graphene structure, it is necessary to couple the phenomenological model of graphene conductivity with Maxwell's equations. The major

challenge here is to model an infinitesimally thin graphene layer using a finite-size discretization of space typical for numerical calculations.

There are two main methods that can be used to model a graphene sheet. The first technique consists in approximating a graphene layer by an equivalent thin slab with a small, but finite, width. The propagation of the electromagnetic fields within the slab is modeled by assigning to it a normalized effective conductivity [4,7]

$$\vec{\sigma} = \begin{pmatrix} \sigma/\Delta & 0 & 0 \\ 0 & \sigma/\Delta & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \dots(2)$$

where D is the thickness of the equivalent slab and the graphene sheet is located in the x - y plane.

The main drawback of this method is that a realistic model of graphene will have a length L much larger than its thickness D , resulting in a very high aspect ratio ($L/D = 1000$). The numerical computation of the electro-magnetic fields in such a structure will therefore require a very high mesh density, leading to a high computational cost.

As an alternative to treat this problem with lower computational costs, the graphene sheet can be modeled as an equivalent impedance surface [13,17]. The surface impedance Z_s connects the tangential component of the

electric field on the surface with the electric surface current, $\mathbf{E}_\tau|_{z=0} = Z_s \mathbf{J}_{surf}$. Taking into account that the current induced in the graphene layer is purely superficial and it is related to the tangential component of the electric field via the surface conductivity $\mathbf{J}_{surf} = \sigma \mathbf{E}_\tau|_{z=0}$, as one can define the boundary conditions at the graphene interface

$$\hat{\mathbf{n}} \times [\mathbf{H}|_{z=+0} - \mathbf{H}|_{z=-0}] = \mathbf{J}_{surf} = \frac{1}{Z_s} \mathbf{E}_\tau|_{z=0} \quad \dots(3)$$

where $Z_s = 1/s$ is the equivalent surface impedance

of the graphene. The boundary conditions (3) fully determine the electromagnetic problem and can be solved numerically using a computational scheme of choice. Fig. 3 contains a comparison between the equivalent slab model and the surface impedance model. In all numerical calculations the method of moments with surface equivalence principle [18] has been employed. The solid lines show the extinction cross section (see Section 4 for details) of the antenna as a function of frequency when the antenna is modeled as a thin slab, with an

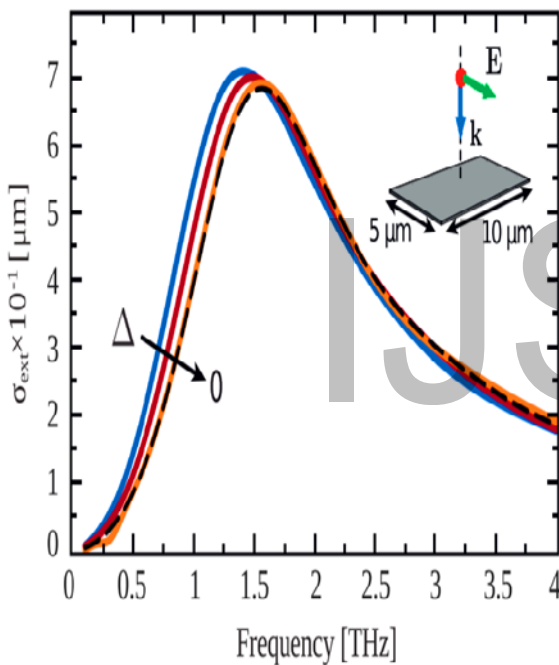


Fig. 3. Extinction cross section per unit width of a 10 mm wide graphene patch with length $L = 5$ mm. Results of the surface impedance model (dashed black line) and the equivalent slab model (solid lines) are shown at room temperature ($T = 300$ K) and zero electrostatic bias ($\mu c = 0$ eV). The thicknesses of the equivalent graphene slab D are 500 nm, 200 nm and 5 nm, from left to right.

effective conductivity as defined in (2), for different antenna thicknesses: 500 nm, 200 nm and 5 nm, from left to right. The dashed line corresponds to the surface impedance model. One can see that the equivalent slab model converges to the surface impedance model as the equivalent slab thickness is reduced, while simultaneously requiring denser mesh (higher computational costs) for smaller equivalent thickness. In what follows the surface impedance model is used to numerically characterize the graphene patch due to its accuracy and efficiency.

4. Novel Graphene Scattering properties

In order to study the performance of a graphene-based nano-patch antenna, it is interesting to investigate the scattering, absorption and extinction cross sections of a graphene patch. The scattering (absorption) cross section is defined as a ratio of the scattered (dissipated) power to the incident power, namely

$$\sigma_{\text{scat}} = \frac{\oint_S d^2r \mathbf{S}_s \cdot \mathbf{n}}{|\mathbf{S}_{\text{inc}}|} \quad \dots(4)$$

and

$$\sigma_{\text{abs}} = \frac{\oint_S d^2r \mathbf{S} \cdot \mathbf{n}}{|\mathbf{S}_{\text{inc}}|} \quad \dots(5)$$

Here the surface integration is performed over a surface enclosing the graphene antenna. \mathbf{n} is the surface normal. \mathbf{S} , \mathbf{S}_s and \mathbf{S}_{inc} are the Poynting vectors of the total, scattered and incident fields, respectively. The extinction cross section is given by the sum of the scattering and the absorption cross sections.

$$\sigma_{\text{ext}} = \sigma_{\text{scat}} + \sigma_{\text{abs}} \quad \dots(6)$$

The calculated scattering and absorption cross

sections of a graphene patch with length $L = 1$ mm and width $W = 100$ mm normalized to the patch geometrical area are shown in Fig. 4. The antenna is supported by an infinite silicon substrate with dielectric constant $\epsilon = 11.9$. Room temperature ($T = 300$ K) and zero electrostatic bias ($\mu_c = 0$ eV) are assumed. The interaction of the terahertz radiation with the antenna is dominated by the absorption, with the scattering being three orders of magnitude weaker due to the large wavelength mismatch between the electromagnetic excitation in the graphene layer and in the far-field.

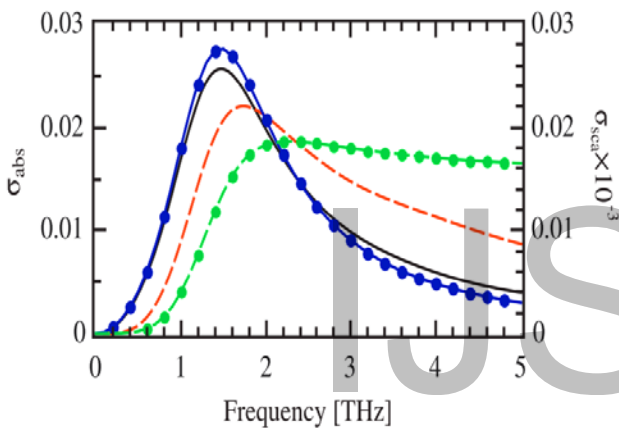


Fig. 4. The absorption (black line) and scattering (dashed red line) cross sections of a graphene antenna on an infinite silicon substrate, obtained using numerical simulations, as compared with the absorption (blue line with dots) and scattering (dashed green line with dots) cross sections obtained using the Fabry–Perot model. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of the article.)

The total extinction cross section is equal to a few percents of the graphene area and demonstrates a clear resonant character. The obtained absorption cross sections are consistent with experimental

results reported for graphene micro-ribbon arrays [19].

In order to understand the resonant behavior, we consider a simple Fabry–Perot (FP) model for the graphene patch. An infinite graphene layer placed on the air-dielectric interface supports transverse-magnetic (TM) SPP waves with a dispersion relation given by [5]

$$\frac{1}{\sqrt{\beta^2 - \frac{\epsilon_0^2}{c^2}}} + \frac{\epsilon}{\sqrt{\beta^2 - \epsilon \frac{\omega^2}{c^2}}} = -i \frac{\sigma(\omega)}{\omega \epsilon_0}, \quad \dots\dots(7)$$

where b and v are the wave-vector and frequency of the SPP wave and ϵ is the dielectric constant of the sub-strate. While the air-dielectric interface does not support SPP waves, a termination of the graphene film acts as a mirror and a FP type resonator can be realized when the following condition is satisfied.

$$L_{eff} = L + 2\delta L = m \frac{\lambda}{2} = m \frac{\pi}{\beta} \quad \dots\dots(8)$$

field penetration outside the graphene patch. Solving the dispersion relation (7) with the FP condition (8) for a given effective resonator length L_{eff} results in a set of m complex frequencies ω_m (resonator modes). The coupling of the incident radiation with those modes leads to resonances in the extinction spectra. Taking into account that the modes of the resonator are orthogonal, one can model them as a set of independent driven harmonic oscillators with angular frequencies

$$\omega_{0m} = \sqrt{(\text{Re}\omega_m)^2 + (\text{Im}\omega_m)^2}$$

Introducing the dipole polarizabilities of the oscillators as

$$\vec{\mu}_m = \frac{f_m}{\omega_{0m}^2 - \omega^2 - i\gamma_m\omega} \mathbf{E}_{inc} = \alpha_m \mathbf{E}_{inc},$$

.....(9)

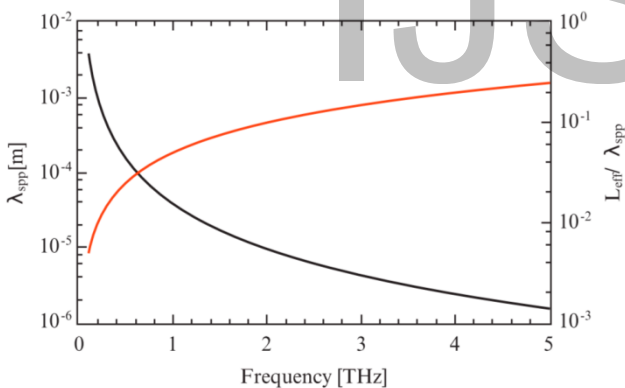
with f_m being the oscillator strength, the scattering and absorption cross sections of the graphene antenna can be calculated as a sum of the normalized scattered and dissipated power of individual oscillators [20], namely

$$\sigma_{sca} = \frac{\omega^4}{6\pi\epsilon_0^2 c^4} \sum_{m=1}^N |\alpha_m|^2 \quad \dots\dots(10)$$

and

$$\sigma_{abs} = \frac{\omega}{\epsilon_0 c} \sum_{m=1}^N \text{Im}\alpha_m \quad \dots\dots(11)$$

In Fig. 4, the absorption and scattering cross sections obtained with the FP model are compared with the results of a direct numerical simulation. The effective length of the FP resonator is set to $L_{eff} = 1.36$ mm, where the penetration length $dL =$



0.18 mm has been estimated based on the numerical simulations. With the oscillator strength f_m used as a fit parameter, a reasonable agreement with numerical results can be achieved even if only the first FP mode ($f_1 = 0.073$) is taken into account. While the operation of the graphene patch antenna is based on the SPP resonances, it is important to analyze the SPP properties. In Fig. 5 the SPP wavelength is shown as a function of the frequency. One can see that in the terahertz

frequency range the wavelength of SPP is of the order of a few micrometers, matching the expected size of envisaged graphene-based nano-antennas. In the same time, the propagation length, shown in **Fig. 5 in units of the corresponding SPP wavelength, is relative small, staying below one SPP wavelength. This result is consistent with the SPP behavior observed at infrared frequencies [21]. However, since a resonant graphene patch antenna will have dimensions of approximately half the SPP wavelength, the sub-wavelength propagation length, due to ohmic losses in the graphene sheet is not expected to hamper the performance of graphene antennas considerably.**

5. Scattering Factor and Tuning

The spectral position of the SPP resonance can be adjusted by an appropriate choice of the resonator length and width. The dependence of the resonant frequency on the resonator length, calculated using equivalent surface impedance method, is shown in Fig. 6 for different resonator widths. The results correspond to a graphene patch on infinite silicon substrate at room temperature and zero electrostatic bias. A wide frequency range in the terahertz band can be covered by choosing antenna dimensions. For a given length, antennas with smaller width possess resonance at lower frequencies. This effect might be attributed to the higher confinement of surface plasmons in a narrow graphene patch, which in turn leads to higher effective permittivity and lower resonance frequency. In the same time, the resonance shifts towards higher frequencies for shorter antennas, in full agreement with the resonance condition (8). The dielectric constant and thickness of the substrate influence both the spectral position and magnitude of

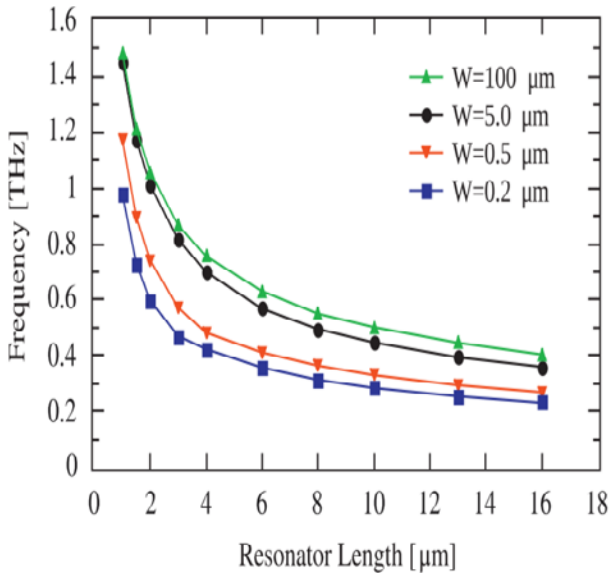


Fig. 6. Dependence of the first resonant frequency of the graphene antenna on its length, L, for different widths, W = 100 mm, W = 5 mm, W = 0.5 mm and W = 0.2 mm.

the resonance. In Fig. 7 (top), the extinction cross section of the graphene antenna with length $L = 1$ mm and width $W = 0.5$ mm supported by different infinite substrates is shown. As expected from the SPP dispersion relation (7), an increase of the dielectric constant of the substrate shifts the resonance toward lower frequencies, while simultaneously reducing the extinction efficiency. For a silicon substrate, a fourfold reduction of the total extinction cross section can be observed in comparison to the antenna suspended in air. One can partially compensate this reduction by adjusting the substrate thickness. In Fig. 7 (bottom), the extinction cross section is shown for the antenna on silicon substrate with different thicknesses. Due to constructive interference in the substrate, the extinction cross section can restore its value corresponding to the antenna in air. In particular, if the FP resonance of the substrate coincides with the one of the antennas ($D = 37.5$ mm), a fivefold

enhancement of the extinction cross section can be achieved.

The strong dependence of the graphene conductivity on the chemical potential μ_c opens the possibility to tune the antenna resonant frequency. In Fig. 8, the extinction cross section of the graphene antenna for different values of μ_c is shown. A chemical potential of 0.2 eV results in the resonant frequency shift of 1.4 THz, while corresponding to a bias field below 1 V/nm which is experimentally feasible and can be achieved with a bias voltage well below 100 V [11]. This could enable a highly tunable antenna in the terahertz band. At the same time, such an antenna would also possess high temperature stability. For the

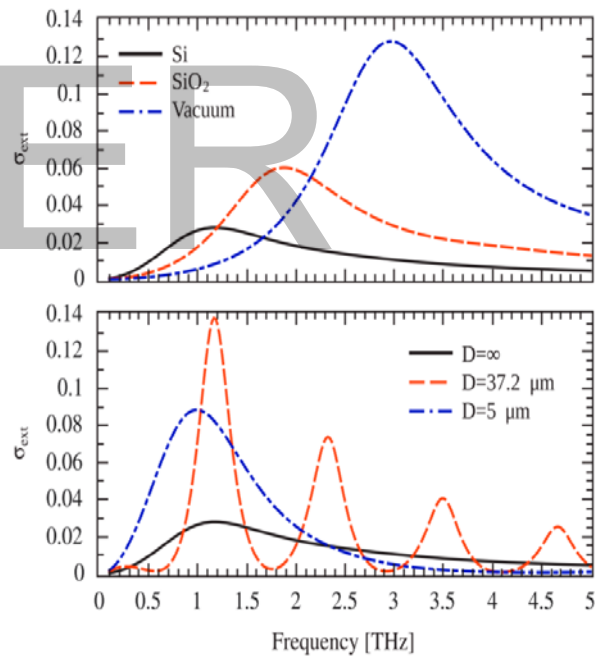
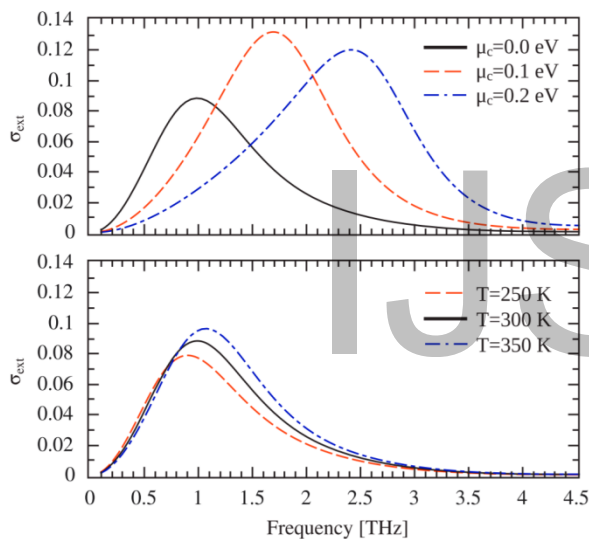


Fig. 7. Top: normalized extinction cross section of the graphene antenna placed on different substrates, silicon ($\epsilon=11.9$), silica ($\epsilon=4.0$) and vacuum (left to right). Bottom: normalized extinction cross section for different thickness of silicon substrates, $D = 1$ (solid), $D = 37.5$ mm (dashed) and $D = 5$ mm (dashed-dotted).

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considered structure, a 100 K temperature variation results in a resonant frequency shift of only 0.15 THz (Fig. 8).

6. Conclusions

To conclude, we have analyzed the radiation scattering on a rectangular graphene-based nanopatch antenna. Due to the propagation of surface-plasmon polariton waves in graphene, the antenna shows a resonant behavior in the terahertz frequency band. Moreover, the simulation results demonstrate that such a structured graphene film has the potential to be used as a tunable terahertz

antenna. Indeed, we have observed that the antenna resonant frequency can be tuned by changing the substrate material or size, or by applying an external electrostatic bias.

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